

$$\mathcal{L}\{1\} = \frac{1}{s}$$

$$\mathcal{L}\{t^n\} = \frac{n!}{s^{n+1}}$$

$$\mathcal{L}\{e^{at}\} = \frac{1}{s-a}$$

$$\mathcal{L}\{t^n e^{at}\} = \frac{n!}{(s-a)^{n+1}}$$

$$\mathcal{L}\{\sin(bt)\} = \frac{b}{s^2 + b^2}$$

$$\mathcal{L}\{\cos(bt)\} = \frac{s}{s^2 + b^2}$$

$$\mathcal{L}\{\sinh(bt)\} = \frac{b}{s^2 - b^2}$$

$$\mathcal{L}\{t \sin(bt)\} = \frac{2bs}{(s^2 + b^2)^2}$$

$$\mathcal{L}\{e^{at} \sin(bt)\} = \frac{b}{(s-a)^2 + b^2}$$

$$\mathcal{L}\{\cosh(bt)\} = \frac{s}{s^2 - b^2}$$

$$\mathcal{L}\{t \cos(bt)\} = \frac{s^2 - a^2}{(s^2 + b^2)^2}$$

$$\mathcal{L}\{e^{at} \cos(bt)\} = \frac{s-a}{(s-a)^2 + b^2}$$

Laplace Transforms For You!

$$\mathcal{L}\{f(t)\} = \int_0^\infty e^{-st} f(t) dt = F(s)$$

$$\mathcal{L}\{\ln t\} = \frac{-\gamma - \ln s}{s}$$

$$\mathcal{L}\{t^r\} = \frac{\Gamma(r+1)}{s^{r+1}}, r > -1$$

$$\mathcal{L}\{t^{n-\frac{1}{2}}\} = \frac{1 \cdot 3 \cdot 5 \cdots (2n-1) \sqrt{\pi}}{2^n s^{n+\frac{1}{2}}}$$

$$\mathcal{L}\left\{\frac{e^{at} - e^{bt}}{t}\right\} = \ln\left(\frac{s-b}{s-a}\right)$$

$$\mathcal{L}\left\{\frac{\sin(bt)}{t}\right\} = \frac{\pi}{2} - \tan^{-1}\left(\frac{s}{b}\right)$$

$$\mathcal{L}\left\{\frac{1 - \cos(bt)}{t}\right\} = \frac{1}{2} \ln\left(1 + \frac{b^2}{s^2}\right)$$

$$\mathcal{L}\{\mathcal{U}(t-a)\} = \frac{e^{-as}}{s}$$

$$\mathcal{L}\{\Pi_{a,b}(t)\} = \frac{e^{-as} - e^{-bs}}{s}$$

$$\mathcal{L}\{\delta(t-a)\} = e^{-as}$$

$$\mathcal{L}\{af(t)\} = aF(s)$$

$$\mathcal{L}\{f(at)\} = \frac{1}{a} F\left(\frac{s}{a}\right)$$

$$\mathcal{L}\{e^{at} f(t)\} = F(s-a)$$

$$\mathcal{L}\{tf(t)\} = -\frac{d}{ds}(F(s))$$

$$\mathcal{L}\left\{\frac{f(t)}{t}\right\} = \int_s^\infty F(u) du$$

$$\mathcal{L}\{t^n f(t)\} = (-1)^n \frac{d^n}{ds^n}(F(s))$$

$$\mathcal{L}\{f(t-a)\mathcal{U}(t-a)\} = e^{-as} \mathcal{L}\{f(t)\}$$

$$\mathcal{L}\{f(t)\mathcal{U}(t-a)\} = e^{-as} \mathcal{L}\{f(t+a)\}$$

$$\mathcal{L}\{f(t)*g(t)\} = F(s)G(s)$$

$$\mathcal{L}\left\{\int_0^t f(v) dv\right\} = \frac{F(s)}{s}$$

$$\mathcal{L}\{f'(t)\} = sF(s) - f(0)$$

$$\mathcal{L}\{f''(t)\} = s^2 F(s) - sf(0) - f'(0)$$

$$\mathcal{L}\{f^{(n)}(t)\} = s^n F(s) - s^{n-1} f(0) - s^{n-2} f'(0) - s^{n-3} f''(0) - \dots - sf^{(n-2)}(0) - f^{(n-1)}(0)$$

You're Welcome!

brdr

$$\Gamma(x) = \int_0^\infty t^{x-1} e^{-t} dt$$

$$\delta(t-a) = \begin{cases} \infty & \text{if } t=a \\ 0 & \text{otherwise} \end{cases}$$

$$\mathcal{U}(t-a) = \begin{cases} 1 & \text{if } t > a \\ 0 & \text{if } t < a \end{cases}$$

$$\Gamma(n) = (n-1)!$$

$$\int_{-\infty}^\infty f(t) \delta(t-a) dt = f(a)$$

$$\Pi_{a,b}(t) = \begin{cases} 1 & \text{if } a < t < b \\ 0 & \text{otherwise} \end{cases}$$

$$\left(\frac{1}{2}\right)! = \frac{\sqrt{\pi}}{2}$$

$$\int_{-\infty}^\infty e^{-x^2} dx = \sqrt{\pi}$$

$$\Pi_{a,b}(t) = \mathcal{U}(t-a) - \mathcal{U}(t-b)$$

$$\gamma = \lim_{n \rightarrow \infty} \left(-\ln n + \sum_{k=1}^n \frac{1}{k} \right)$$

$$\int_{-\infty}^\infty \frac{\sin x}{x} dx = \pi$$

$$f(t)*g(t) = \int_0^t f(t-v)g(v)dv$$